
Cryptography: How Math Keeps the Internet Safe

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Introduction: Secrets in the Code

Every time you send a message, make an online purchase, or log into your email, there's a silent guardian working behind the scenes: mathematics.

From WhatsApp chats to bank transfers, the digital world relies on cryptography — the ancient science of keeping secrets. But unlike spies with invisible ink, today's secret-keepers use complex math to lock data away from prying eyes.

In this blog, we'll uncover how mathematics powers modern cryptography, turning numbers into armor that protects our online lives.

Keywords: Cryptography, Encryption, Decryption, Internet security, RSA Algorithm.

What Is Cryptography?

At its core, cryptography is the study and practice of secure communication.

It involves:

- Encrypting a message (scrambling it)
- Decrypting it (unscrambling it)
- Ensuring that only the intended recipient can read it

Cryptography transforms readable information (plaintext) into unreadable gibberish (ciphertext) using algorithms and keys — all based on math.

A Brief History of Secrecy

Ancient Encryption

- Caesar Cipher: Shift each letter by a fixed number (e.g., $A \rightarrow D$)
- Scytale (Sparta): A message wrapped around a rod, readable only with the correct diameter

These were clever but easy to crack. Modern encryption? Light-years ahead.

Modern Cryptography

With the rise of computers, encryption became *mathematical* — not just linguistic. Now, it's based on number theory, prime factorization, and modular arithmetic.

The Math Behind Modern Cryptography

1. Prime Numbers

Modern encryption, like RSA (Rivest–Shamir–Adleman), depends on the difficulty of factoring large numbers into primes.

Why? Because multiplying two large primes is easy. But figuring out what they were from the product? Practically impossible without enormous computing power.

Example: Multiplying 53×97 is straightforward, but can the process be reversed when only the product 5141 is provided?

This mathematical asymmetry is what makes RSA secure.

2. Modular Arithmetic

Think of clocks: 13 o'clock = 1 o'clock. That's modular math.

This helps scramble messages into seemingly random outputs that can only be reversed with the right key.

3. Hash Functions

A hash function converts data into a fixed-size string (like a fingerprint). You can't reverse it — that's the point.

Used in:

- Password storage
- File integrity verification
- Blockchain systems like Bitcoin

4. Elliptic Curve Cryptography (ECC)

Instead of giant primes, ECC uses elliptic curves — complex algebraic equations — to create secure keys with smaller data sizes. It's faster and more efficient, especially for mobile devices.

Where Cryptography Shows Up in Real Life

Online Banking

When you type your credit card number, it's encrypted before it leaves your browser. Without decryption, it's meaningless to hackers.

Messaging Apps

Apps like WhatsApp and Signal use end-to-end encryption — only your device and the recipient can decrypt messages. Not even the app company can read them.

Digital Signatures

Used to verify identity in emails, contracts, and even software downloads. They prove the message came from a trusted source and hasn't been altered.

Blockchain & Cryptocurrency

Bitcoin and other cryptocurrencies are built entirely on cryptographic principles — from transaction validation to wallet protection.

The Future: Quantum Threats & Post-Quantum Cryptography

Quantum computers could one day break current cryptographic methods — especially those based on prime factorization.

That's why researchers are racing to develop post-quantum cryptography — algorithms secure against quantum attacks, using:

- Lattice-based cryptography
- Multivariate equations
- Code-based schemes

The next encryption era is already on the horizon.

Conclusion: Math = Digital Armor

Cryptography shows us the power of pure math in the real world — not just in classrooms, but in every tap, swipe, and click.

From ancient scrolls to AI-powered banking apps, the mission has always been the same: protect the message. And math is still the most trustworthy shield we have.

So the next time you see a padlock in your browser bar, know that you're watching a centuries-old battle of logic and secrecy — won by clever numbers.